Effects of an Early Intervention for Second Grade Students At-risk for Mathematics Difficulties

Council for Exceptional Children April 2011 Diane P. Bryant and Brian R. Bryant Greg Roberts, Kathleen Pfannenstiel, Jennifer Porterfield The University of Texas at Austin: Mathematics Institute for Learning Disabilities and Difficulties

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#### **Background and Rationale**

5% to 8% of school-age children exhibit some form of mathematics disability  Individuals with
 Disabilities
 Education
 Improvement
 Act (2004)
 emphasizes
 prevention
 and
 intervention Identification of students with MD Validation of assessments and multitiered interventions aimed at prevention



### Theoretical & Conceptual Framework

#### Number, Operation, and Algebra

- Number sense (e.g., numerical values of small quantities, basic counting skills, numeral recognition) develop informally prior to starting school and through more formal instruction in school (National Mathematics Advisory Panel [NMAP], 2008; National Research Council [NRC], 2001, 2009).
- Whole number concept development and proficiency should be the critical foundation of mathematics intervention for preventative intervention; foundation for algebra (NMAP, 2008)

#### Mathematical Models/Representations

• Representations (concrete, pictorial, symbolic/abstract) help students develop and build mathematical understanding of concepts, operations, relations, and properties (Bryant et al., 2008, in press; Gersten et al., 2009; NRC, 2001).

FOR PREVENTING EDUCATIONAL RISK

#### **Research Question**

• What are the effects of the Tier II Early Numeracy Booster (ENB) supplemental intervention delivered by trained tutors on the mathematics performance of at-risk second grade students when compared to the mathematics performance of at-risk students who are receiving "standard practice" mathematics instruction in general education classrooms?

#### Study Demographics (Two Cohorts, Years 1 and 2)

0	Intervention (N	Comparison ( $N = 51$ )	Total (N = 1427)
	= 108)		
Tested:			
Fall	108 = 100 %	51 = 100 %	1354 = 94.9 %
Winter	104 = 96.3 %	50 = 98 %	1360 = 95.3 %
Spring	105 = 97.2 %	50 = 98 %	1338 = 93.8 %
Gender:			
Male	42 = 38.9 %	29 = 56.9 %	733 = 51.4 %
Female	66 = 61.1 %	22 = 43.1 %	690 = 48.4 %
Missing			4 = .28 %
Ethnicity:			
Asian/Pacific Islander	4 = 3.7 %	2 = 3.9 %	163 = 11.4 %
African-American	29 = 26.9 %	9 = 17.6 %	280 = 19.6 %
Caucasian	40 = 37 %	15 = 29.4 %	538 = 37.7 %
Hispanic	35 = 32.4 %	25 = 49 %	424 = 29.7 %
Missing			19 = 1.3 %
Free/Reduced Lunch	52 = 48.1 %	24 = 47.1 %	505 = 35.4 %
English Language Learner	5 = 4.6 %	7 = 13.7 %	210 = 14.7 %



#### Measures: Texas Early Mathematics Inventories-PM (available free to Texas educators)

4 subtests: Magnitude Comparisons, Number Sequences, Place Value, Addition/Subtraction Combinations (2 minutes each)

Aggregate Total Score (TS) of four subtests used to measure fall, winter, and spring student performance –most robust indicator of performance of the four constructs

Alternate forms reliability - immediate test/retest: subtest coefficients ranged from .76 to .81, TS = .89



#### **Number Sequences**

• Placement

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• Decade effects

297	298	_	_	201	202	298		300
335	_	337	307	308		_	429	430
336	337	_		313	314	469		471
406	_	408	_	500	501	554	555	_
_	457	<b>4</b> 58	565	566		568	569	_
								-

#### **Magnitude Comparisons**

- Place value
- Distance effect
- Compatibility

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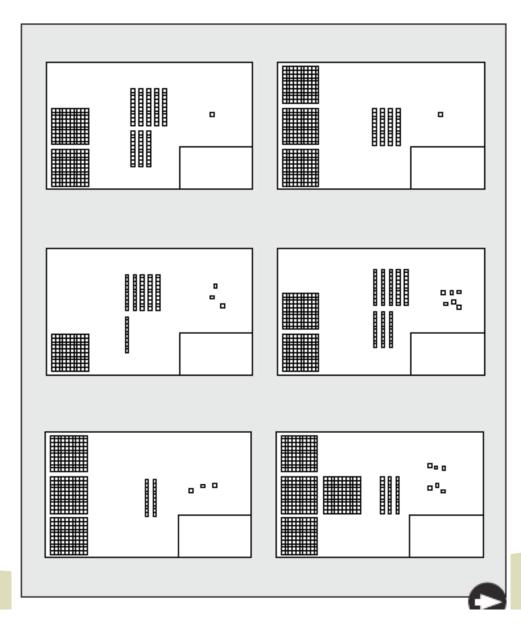
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62 69	47 17	53 482	241 270
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207 424	431 428	440 318	l66 2l3
u22 201	104 841	1115 720	201 521
433 291	104 841	145 729	381 531
64I I35	610 278	945 945	467 524



#### **Place Value**

- Counting
- Subitizing
- Switching



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#### **Addition/Subtraction Combinations**

• Fingers

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• Strategies

7	10	4	8
7	_ 4	+ 7	+ 4
6	10	6	7
+ 6	_ 5	_ 5	+ 7
7	9	3	15
+ 4	- 8	+ 8	6

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# How do we report Benchmark Check results?

Easy as A-B-C

Insert student TEMI-PM Total Scores.															
		MC			NS			PV			ASC		Total Score		
Student Name	Fall	Winter	Spring	Fall	Winter	Spring									
Angelo	- 15	16	28	9	10	20	2	- 4	- 11	6	6	20	32	58	79
Christian	48	62	64	20	29	- 31	9	17	- 21	26	35	40	103	183	156
Emly	24	42	45	5	21	20	8	12	16	16	24	12	53	127	93
Haylee	22	35	39	- 5	16	21	- 5	8	9	5	15	13	37	100	82
Jaimie	41	52	56	12	17	22	7	9	9	13	12	10	73	119	97
John	43	47	56	16	21	27	- 11	- 11	17	26	30	- 31	96	147	131
Jonathan	39	52	58	15	17	19	9	12	15	17	22	29	80	131	121
Julie	12	20	30	4	8	13	4	7	9	- 5	5	13	25	57	65
Kaithlyn	34	35	38	9	14	18	5	7	9	15	21	22	63	100	87
Mae	41	55	62	- 14	19	20	12	13	18	16	21	27	83	140	127
Michelle	20	25	42	2	10	16	1	6	9	8	15	26	- 31	73	93
Stepanie	27	40		13	20		8	12		19	29		67	109	
Steve	21	28	31	0	12	13	5	7	8	- 11	17	22	37	82	74
Tim	30	41	51	13	16	18	8	9	13	16	24	20	67	116	102
Victor	20	34	35	10	13	9	5	5	6	13	16	14	48	82	64
Class Averages	29	- 39	45	10	16	19	- 7	9	12	- 14	19	- 21	60	108	98
Total Students Tested	15	15	14	15	15	14	15	- 15	14	15	15	14	- 15 -	- 15	14
vanher of Students Below 25th Percentile	2	3	3	- 5	4	3	3	6	9	0	2	2	3	2	3
% of Students Below 25th Percentile	13%	20%	21%	33%	27%	21%	20%	40%	64%	0%	13%	14%	20%	13%	21%
Weeks 32-40 25th Percentile Line	29		32	10		16	7		14	14		13	60		- 17

#### **Reporting Results for Teachers MS Access**

exas Early Math Student R			ntories	Name: Alex Vargas School: Example Teacher: Sample
gress Monitoring				
lagnitude Comparisons		Benchmark	Score	Rating
omparing two numbers'	Fall	27	32	Exceeded Benchmark - Average
uantity (0 to 999)	Winter	34		
	Spring			
lumber Sequences		Benchmark	Score	Rating
Identifying the missing number in a three number sequence (0 to 999)	Fall	10	11	Exceeded Benchmark - Average
	Winter	15		
	Spring	15		
Place Value		Benchmark	Score	Rating
ace Value	Fall	6	8	Exceeded Benchmark - Average
f hundreds, tens, and ones (0	Winter	8		
o 999)	Spring	11		-
ddition/Subtraction		Benchmark	Score	Rating
Combinations	Fall	14	16	Exceeded Benchmark - Average
nowing the basic addition	Winter	21		
nd subtraction facts	Spring	24		а С. С. С
EMI-PM Total Score		Benchmark	Score	Rating
	Fall	58	67	Exceeded Benchmark - Average
Inderstanding number, wantity, and operations TEKS	Winter	80		
	Spring	92		

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# **Objectives of Intervention by Area**

<ul> <li>Ordering and Comparing Numbers:</li> <li>Students will identify, write, count and decompose numbers</li> <li>Students will order (greatest- least &amp; least-greatest) two &amp; three-digit numbers</li> <li>Students will identify and write the missing number</li> <li>Students will identify numbers from a variety of representations (number line, hundreds chart, concrete, pictorial)</li> </ul>		Unit: Instruc 1: 0-50 2: 0-100 3: 0-200	etional Content 6: 0-500 7: 0-700 8: 0-800	
<ul> <li><u>Place Vale:</u></li> <li>Students will identify, write, count and decompose numbers</li> <li>Students will identify the number that is more than/less than/equal to, when given two numbers</li> <li>Students will identify the ones, tens and hundreds place of two-digit numbers</li> <li>Students will make numbers using a variety of representations (concrete, pictorial)</li> </ul>		4: 0-300 5: 0-400 Unit	9: 0-900 10: 0-999 : Strategy	
Addition & Subtraction Facts: • Students will identify, write and decompose numbers • Students will identify and define the operational signs in problems (+, - and =) • Students will identify the three-numbers in a fact family • Students will write number sentences for fact families • Students will identify the type of problem and solve using the appropriate strategy	2: 3: 4:		6: Fact Families e 7: Double Facts 8: Doubles +1 9: Make Ten, Ten +More 10: Make Ten +More	
<ul> <li>Word Problem Solving:</li> <li>Students will identify, write, count and decompose numbers</li> <li>Students will identify important numbers and words needed to solve the problem</li> <li>Students will identify the unit and write a number sentence to solve</li> <li>Students will check work by writing and solving the related number sentence</li> <li>Students will solve problems using a variety of representations (concrete, pictorial)</li> </ul>	2 1 3 1 2 7	: Strategy Instruction 2: Joining, result Inknown 3: Separate, results Inknown 4: Joining/Separate, results Unknown 5: Join/Separate,	on change unknown 6: Result and Chang Unknown 7: Beginning unknov 8: Compare unknov join 9: Compare unknov separate 10: Review	wn vn,

# **Multiple Visual Representations**

- Concrete: Interactive Modeling/Guided Practice
  - Cubes
  - Counters
  - Base-ten/Place value materials (units, rods, flats)
  - Dot cubes
- Pictorial: Guided Practice/Independent Practice
  - Five frames
  - Ten frames
  - Hundreds charts
  - Number lines
- Abstract/Symbolic: Guided Practice/Independent Practice
  - Numbers & Symbols
- Mats (can be used across all representations)
  - Part-part-whole
  - Fact family
  - Strategy mats



#### **Intervention Components**

On Going Progress Monitoring (student response to intervention) Mathematical Models/ Representations to build conceptual understanding (Concrete-pictorialabstract sequence)

Principles of effective instructional design: Sequence of skills and concepts, instructional routine, student engagement, examples



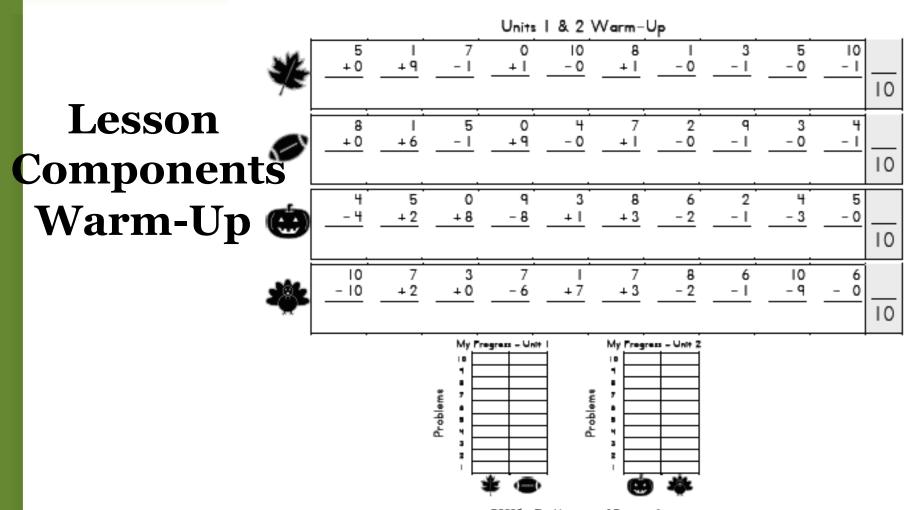
#### **Implementation Components**

Units and lessons: 10 units, eight lessons per unit (representations & content)

Duration: 19 weeks - 4 days per week; 30 minutes each lesson

Grouping: Small groups of 4 -5 students

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# Ordering and Comparing Numbers

	-								
	P				-				
1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100
1	24			26	2	15		1	7
3	46		2	48	4	39		4	1
5	4		(	6	6	68		7	0
7	71		, 	73	8	94		9	6
9	82		8	84	10	79		8	1

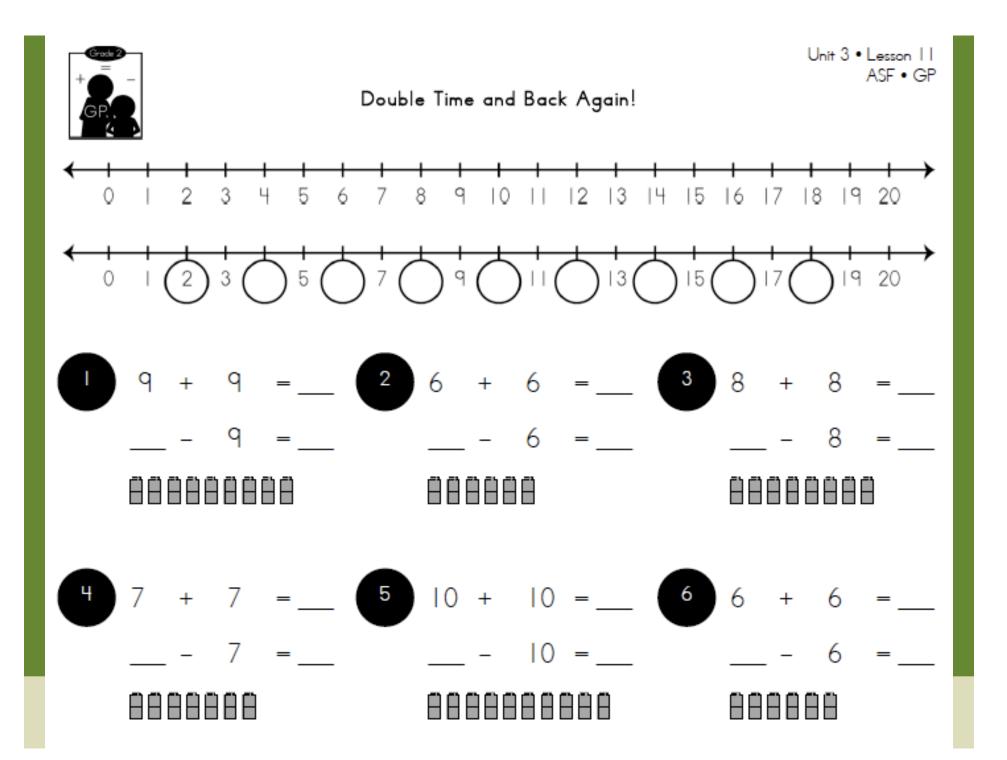


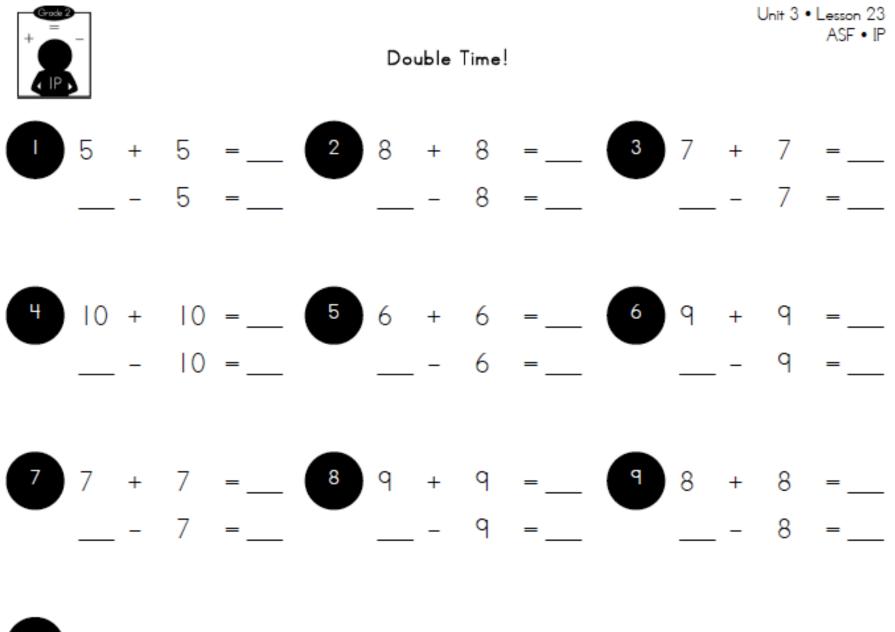
### Addition/Subtraction Facts: Part-Part-Whole-Break-Apart

 Modeled Practice: Concrete Representations/ Models

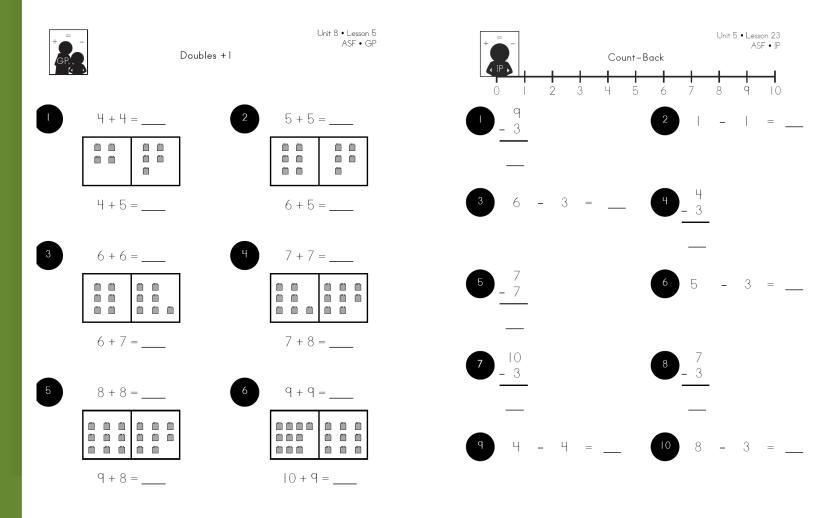








#### Addition/Subtraction Facts: Pictorial-Doubles + 1 & Count Back





### **Addition/Subtraction Facts:** Make 10 + More



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Step 1: Check the fact; is there a 7, 8, or 9 in it? (yes) There is a 9 in this fact.

1. Place the Modeled Practice sheet on the table. Have students look at

their Modeled Practice sheets. Introduce the Make 10 + More

Step 2: Make 10.

strategy, using the fact 9 + 4.

Modeled Practice (My Turn, Your Turn)

**9** plus what equals **10**? (1)

There are 3 steps to remember.

My Turn: I take 1 chip from the group of 4 to put with the group of 9. (Move the counter from the dotted circle along the dotted arrow to the empty box in the top ten frame.)

I know that 9 + 1 = 10. I made 10!

Your Turn: Make 10.

Step 3: 10 + More.

I have 10 in 1 frame, plus 3 remaining chips.

What is 10 + 3? (13)

 $S_0 9 + 4 = 13$ .

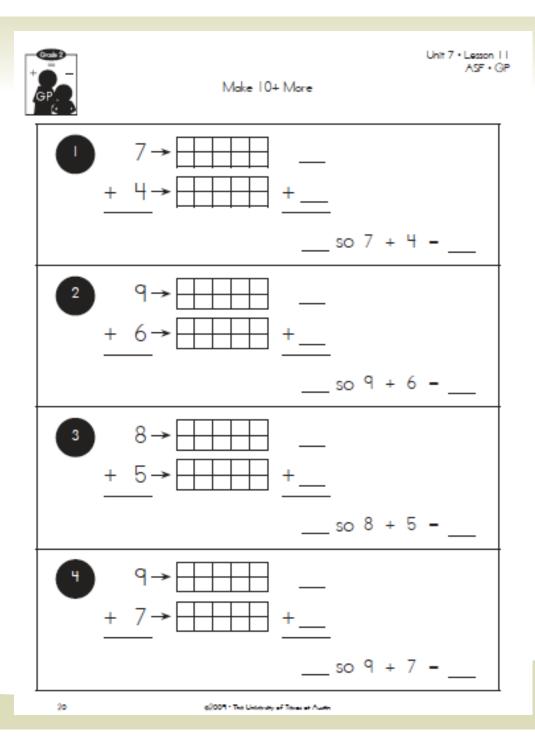
What is the turnaround fact? (4 + 9 = 13)

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### Addition & Subtraction Facts

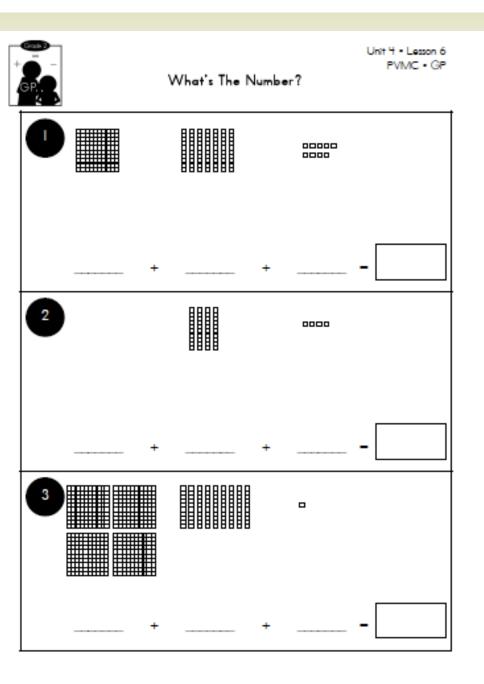


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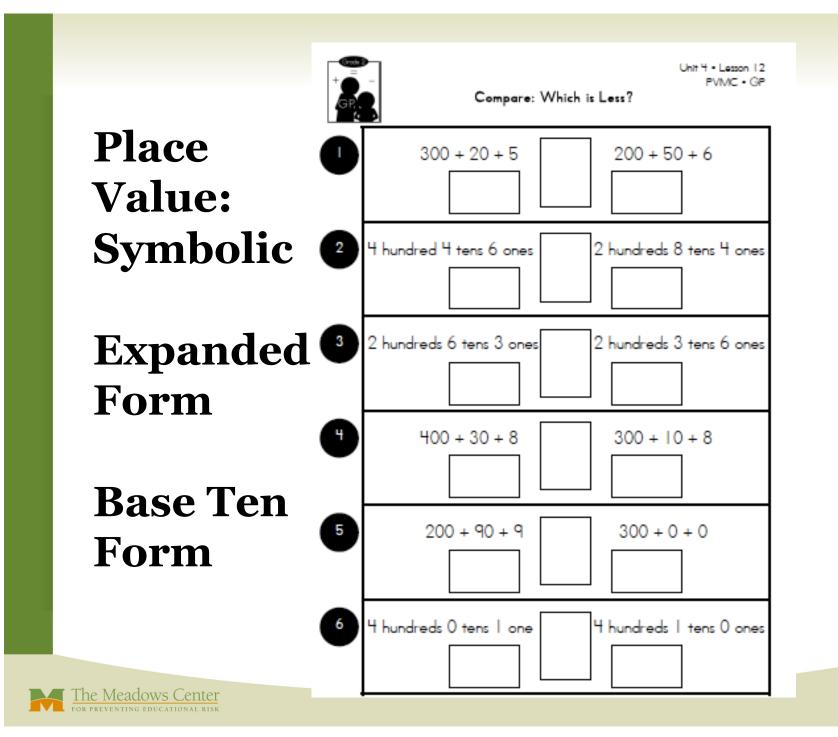
# Place Value: Pictorial

#### Expanded Form

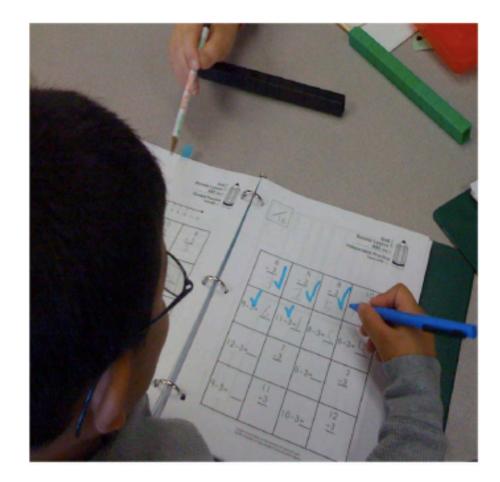




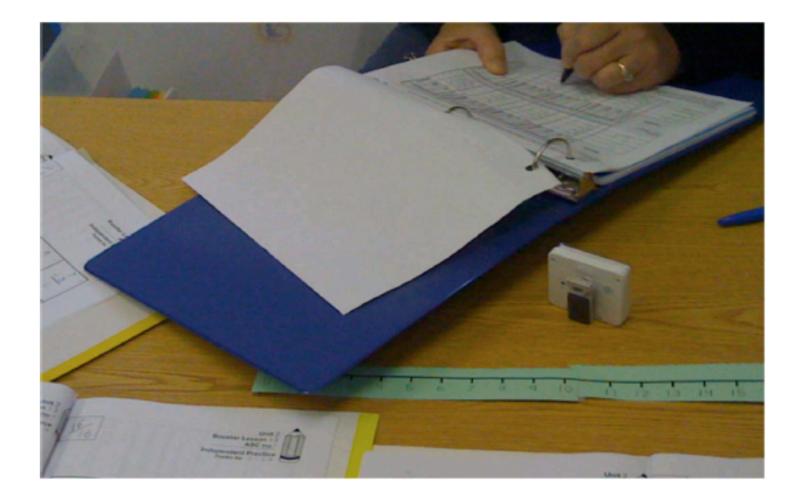
én:







#### Students completing Independent Practice and checking their work.



#### Using daily progress monitoring to track student responses.

# Fidelity

- An observation rating scale was used for datacollection purposes ranging from 3 for Most of the Time to 0 for Not at All.
- Overall = 2.82
- Intervention = 2.95
- Instruction = 2.85
- Monitoring and Managing Behavior = 2.65

# **Instruction for Comparison Students**

- No explicit, systematic mathematics instruction was observed with the comparison students.
- Teachers focused on completing the whole-class assignment in a smaller group, through centers, or by reviewing for upcoming assessments.
- A variety of groupings and instructional materials were observed:
  - small-group instruction to work with the comparison students
  - group size varied from pairs of students, to small groups of three to five students, to larger groups of seven or more
  - manipulatives, worksheets

#### Analyses

- Validated early numeracy timed progress-monitoring measures were used to identify students with risk status and to monitor mathematics performance across the year (fall, winter, spring).
- We combined 2<sup>nd</sup> graders in cohort 1 and cohort 2 to increase the power of the treatment effect analysis.
- ANCOVA was used to evaluate group differences in the spring of 2<sup>nd</sup> grade.
- Benjamani-Hochberg was applied to control for Type 1 error rate.
- Fall scores were used as covariates.



#### **Overall Findings**

Data Analysis											
Scale	F-M	F-SD	S-M	S-SD	F	p	1				
TEMI- MC	29.75 29.26	5.472 4.189	42.20 38.76	10.047 8.019	3.24	.075					
FEMI-NS	9.58 9.89	2.097 2.024	16,16 13.78	5.229 3.409	6.98	.009					
FEMI-PV	6.32 6.18	2.307 2.680	13.77 9.11	3.826 3.089	44.27	.000	1				
A DATA STREET A MOUNT A		2/4040 4: 3050 fox 6100	<ul> <li>Casses of Delevation Uses of all</li> </ul>	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1							

.678 M TEMI .500 TEM 1.280 TEMI-13.91 4.261 23.76 7.340 1.36 .246 .263 ASC 4.957 6.372 13.39 21.89 59.57 5.384 95.90 19.034 TEMI-Tot 11.49 .687 .001 58.74 6.566 83.54 15.038 **SAT-10** 88.94 9.930 0.11 .085 NA NA .738 MPS 88.08 10.079 **SAT-10** 91.29 9.460 NA 0.56 .455 .187 NA MP 80.27 12.965 **SAT-10** 89.15 9.600 NA NA 0.33 .564 .146 87.70 10.338 Tot

\* Unbiased Hedges g



ES\*

#### Results

#### **Overall Findings**

- The treatment group outperformed the comparison on all TEMI-PM measures.
- The differences were statistically significant for number sequences (*p*<.009), place value (*p*<.001), and the PM total score (*p*=.001).
- The Benjamani-Hochberg procedure did not alter the pattern of significant findings.
- There were no statistical differences on the Stanford Achievement Test 10.



#### **Discussion & Implications for Instruction**

Struggling students can benefit from a supplemental intervention that focuses on important foundational concepts and skills (NCTM, 2006; NMAP, 2008).

Future research should examine how to achieve more robust findings with addition and related subtraction facts. Future research should focus on how enhancements in number and operation can translate to improved performance in other mathematical areas.

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